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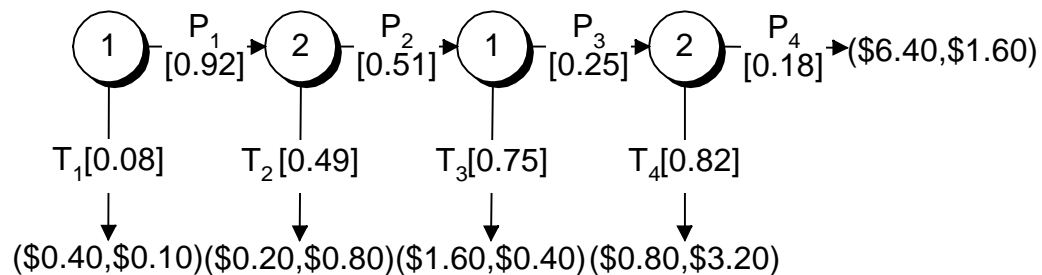
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# **Experimental Economics**

by David K. Levine

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# Centipede Game: Palfrey and McKelvey



Numbers in square brackets correspond to the observed conditional probabilities of play corresponding to rounds 6-10, stakes 1x below.

This game has a unique self-confirming equilibrium; in it player 1 with probability 1 plays  $T_1$

## Summary of Experimental Results

Trials / Rnds	Rnds	Stake	Case	Expected Loss			Max Gain	Ratio
				PI 1	PI 2	Both		
29*	6-10	1x	H	\$0.00	\$0.03	\$0.02	\$4.00	0.4%
29*	6-10	1x	U	\$0.26	\$0.17	\$0.22	\$4.00	5.4%
	WC	1x	H			\$0.80	\$4.00	20.0%
29	1-10	1x	H	\$0.00	\$0.08	\$0.04	\$4.00	1.0%
10	1-10	4x	H	\$0.00	\$0.28	\$0.14	\$16.00	0.9%

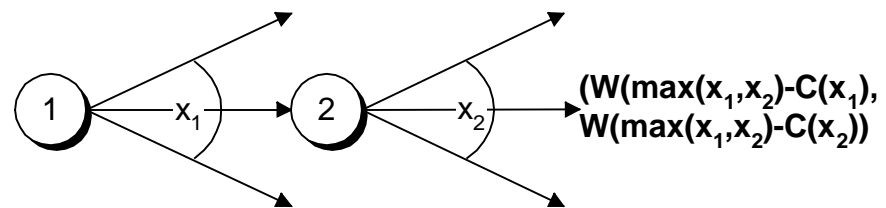
Rnds=Rounds, WC=Worst Case, H=Heterogeneous, U=Unitary

\*The data on which from which this case is computed is reported above.

### *Comments on Experimental Results*

- heterogeneous loss per player is small; because payoffs are doubling in each stage, equilibrium is very sensitive to a small number of player 2's giving money away at the end of the game.
- unknowing losses far greater than knowing losses
- quadrupling the stakes very nearly causes  $\bar{\epsilon}$  to quadruple
- theory has substantial predictive power: see WC
- losses conditional on reaching the final stage are quite large--inconsistent with subgame perfection. McKelvey and Palfrey estimated an incomplete information model where some "types" of player 2 liked to pass in the final stage. This cannot explain many players dropping out early so their estimated model fits poorly.

# Best Shot Game: Prasnikar and Roth



$x$	$W(x)$	$C(x)$
0	\$0.00	\$0.00
1	\$1.00	\$0.82
2	\$1.95	\$1.64
3	\$2.85	\$2.46
4	\$3.70	\$3.28
5	\$4.50	\$4.10
6	\$5.25	\$4.92
7	\$5.95	\$5.74
8	\$6.60	\$6.50

## *Discussion of Best Shot*

if the other player makes any contribution at all, it is optimal to contribute nothing

unique subgame perfect equilibrium player 1 contributes nothing

another Nash equilibrium player 2 contributes nothing regardless of player 1's play

it is not consistent with Nash equilibrium for some player 1's to play 0 and others 4

any other probability distribution over the two Nash equilibria are heterogeneous self-confirming



## Summary of Results from Best Shot

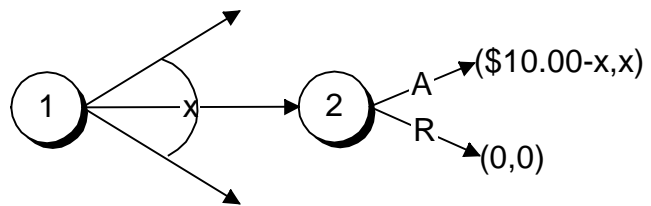
Trials	Rnds	Info	Case	Expected Loss			Max Gain	Ratio
				PI 1	PI 2	Both		
8	8-10	full	H	\$0.00	\$0.12	\$0.06	\$2.06	2.9%
8	8-10	full	U	\$0.00	\$0.12	\$0.06	\$2.06	2.9%
10	8-10	part	H	\$0.01	\$0.15	\$0.08	\$2.06	3.9%
10	8-10	part	U	\$0.39	\$0.15	\$0.27	\$2.06	13.%
	WC		H			\$3.41	\$2.06	165%

Rnds=Rounds, WC=Worst Case, H=Heterogeneous, U=Unitary

## *Comments on Best Shot*

- In the full information case and partial information heterogeneous case player 2 occasionally contributes less than 4 when player 1 has contributed nothing; Note that the player who contributes nothing gets \$3.70 against \$0.42 for the opponent who contributes 4
- larger losses than centipede game with lower stakes
- full information case heterogeneous losses equal unitary losses-- player 1 never contributed anything, and so never had a loss with either type of information; all losses by player 2 are necessarily knowing losses
- In the partial information case occasionally player 1 contributed 4 and player 2 contributed nothing: looks like public randomization between the two Nash equilibria. This is inconsistent with Nash equilibrium but consistent with self-confirming equilibrium.

# Ultimatum Game:



Trials	Rnd	Cntry	Case	Expected Loss			Max Gain	Ratio
				PI 1	PI 2	Both		
27	10	US	H	\$0.00	\$0.67	\$0.34	\$10.00	3.4%
27	10	US	U	\$1.30	\$0.67	\$0.99	\$10.00	9.9%
10	10	USx3	H	\$0.00	\$1.28	\$0.64	\$30.00	2.1%
10	10	USx3	U	\$6.45	\$1.28	\$3.86	\$30.00	12.9%
30	10	Yugo	H	\$0.00	\$0.99	\$0.50	\$10?	5.0%
30	10	Yugo	U	\$1.57	\$0.99	\$1.28	\$10?	12.8%
29	10	Jpn	H	\$0.00	\$0.53	\$0.27	\$10?	2.7%
29	10	Jpn	U	\$1.85	\$0.53	\$1.19	\$10?	11.9%
30	10	Isrl	H	\$0.00	\$0.38	\$0.19	\$10?	1.9%
30	10	Isrl	U	\$3.16	\$0.38	\$1.77	\$10?	17.7%
	WC		H			\$5.00	\$10.00	50.0%

Rnds=Rounds, WC=Worst Case, H=Heterogeneous, U=Unitary

## *Comments on Ultimatum*

- every offer by player 1 is a best response to beliefs that all other offers will be rejected so player 1's heterogeneous losses are always zero.
- big player 1 losses in the unitary case
- player 2 losses all knowing losses from rejected offers; magnitudes indicate that subgame perfection does quite badly
- as in centipede, tripling the stakes increases the size of losses a bit less than proportionally (losses roughly double).

### *Raw US Data for Ultimatum*

<i>x</i>	<i>Offers</i>	<i>Rejection Probability</i>
\$2.00	1	100%
\$3.25	2	50%
\$4.00	7	14%
\$4.25	1	0%
\$4.50	2	100%
\$4.75	1	0%
\$5.00	13	0%
	27	

US \$10.00 stake games, round 10